## Corrections to the book "Linear Time-Varying Systems - Algebraic Analytic Approach" by H. Bourlès and B. Marinescu

- 1. p. v, line 2 from top: read "a été" instead of "à été"
- p. viii, line 7 from top: read [225] instead of [224]
   p. 5,
  - 7th line from top, after  $X'_i \cap X'_j$ , add "=  $\emptyset$ "
  - 3rd line after Definition 3: change  $\prod$  to  $\bigcup$
  - 1st line of §1.2.1.5, after " $\mathcal{R}(x, x')$ ", add "or  $x\mathcal{R}x'$ "
- 4. p. 6, 9th line of §1.2.2.1, change  $\operatorname{Hom}_{\mathcal{C}}(X, X)$  to  $\operatorname{Hom}_{\mathcal{C}}(X, Y)$
- 5. p. 9, before  $\S1.2.2.4$ : delete the sentence in parentheses
- 6. p. 10, lines 12 and 16 from top: read "generator" instead of "cogenerator"
- 7. p. 11, line 6 from top: read "if" instead of "is"
- 8. p. 14,
  - 1st line from top: change " $\mathcal{C} \to \mathcal{C}$ " to " $I \to \mathcal{C}$ , where I stands for the category consisting of the object I alone"
  - 4th line from bottom: change "complete" to "cocomplete"
  - 2nd line from bottom: change  $x_i \mathcal{R} x_j$  to  $x_i \equiv x_j \pmod{\mathcal{R}}$
- 9. p. 15, 1ast line, after "functor", add " $I \rightarrow C$ "
- 10. p. 16, 2nd line after the proof of Proposition 23: change "cocomplete" to "complete"
- 11. p. 26, last line of Lemma and Definition 53, add: "See Lemma 571 below."
- 12. p. 27, 3rd line of Sect. 1.3: suppress a blank and a dot
- 13. p. 41, 4th line of Example 109: change "be" to "is"
- 14. p. 47, Remark 132(a,ii), 2nd line: change M to  $\mathbf{M}$  three times
- 15. p. 51,
  - 2nd line of Item (3) of Theorem and Definition 145: change "then f" to "then  $\bar{f}$ "

• 2nd line from bottom: change g to x two times

- 16. p. 55, 2nd line from top: after "if", add "s = r and"
- 17. p. 57, line 6 from top: after "by", add "f with respect to"
- 18. p. 58, 6th line of (1.6.9.1): change  $\bigcup$  to  $\bigcup$
- 19. p. 60, 3rd line from top, after "limits", add "and continuity"
- 20. p. 62, line 12 from below,
  - add at the beginning of the line "and the converse holds true if  $X[\mathfrak{T}]$  is semicomplete"
  - $\bullet\,$  change "§III.5," to "§III.4, Corol. 1 and"
- 21. p. 65,
  - §1.7.3.4, title: change "Inductive" to Projective Limits and Inductive"
  - Just below, add the following:

Let I be a filtering set and let  $\{X_i [\mathfrak{T}_i], \psi_j^i\}$  be an inverse system with index set I in the category **LCS** (Definition 21). The projective limit  $\lim_{\leftarrow} X_i [\mathfrak{T}_i]$  is defined as usual (Definition 22) and is an LCS  $\overset{\leftarrow}{X} [\mathfrak{T}_{\leftarrow}]$ . This LCS is complete (resp., semicomplete) if, and only if so is each  $X_i [\mathfrak{T}_i]$ . Furthermore, every complete LCS is a projective limit of Banach spaces ([190], 19.9(1), 19.10(2)).

- 22. p. 66, 4rd line from below, add the following sentence at the beginning of the line: "Clearly, as defined above, an  $(\mathcal{FS})$  space is a projective limit of Banach spaces with compact maps  $\psi_j^i = \rho_j^i$ , and dually a  $(\mathcal{DFS})$  space is an inductive limit of Banach spaces with compact maps  $\varphi_j^i = \rho_j^i$ ."
- 23. p. 67,
  - line 16 from bottom: instead of "a ", read "for it is a Schwartz space ([147], §III.4), thus an  $(\mathcal{FS})$  space"
  - line 14 from bottom, at the end of the sentence, add "since from the above it is a (DFS) space"
- 24. p. 68, 2nd line from bottom, after "space.", add: "Furthermore, it can be proved to be an  $(\mathcal{FS})$  space ([149], Chap. 4, Part 4, Corol. 2 of Prop. 5)."
- 25. p. 69, suppress lines 9 and 10 from top
- 26. p. 71,

- 4th line from top: change  $\varphi$  to  $\varphi_n$
- 7th line from top: after change "a" to "an  $(\mathcal{FS})$  space, thus a"
- 9th line from top: after "is", add "a  $(\mathcal{DFS})$  space, thus is"
- Replace the sentence beginning at line 14 by "Therefore" by the following: "The LCS  $\mathcal{D}(X)$   $[\mathfrak{T}_{\rightarrow}^{\infty}]$  and its strong dual  $\mathcal{D}'_{\beta}(X)$  have the same topological properties as  $\mathcal{E}(X)$   $[\mathfrak{T}_{\rightarrow}^{\infty}]$  and  $\mathcal{E}'_{\beta}(X)$ , i.e. they are an  $(\mathcal{FS})$  space and a  $(\mathcal{DFS})$  space, respectively."
- p. 72, 8th line from top: put "22.18.7" in parentheses
- 3rd line from bottom: add a right parenthesis after "(14.1.1)"
- 27. p. 82, 2nd line: change B(X) to  $\mathcal{B}(X)$
- 28. p. 83, 4th line of Exercise 196: change "categories but are" to "but"
- 29. p. 84, in Exercise 199(2), first line: after "be", add "a"
- 30. p. 85, 2nd line from bottom: change S to X
- 31. p. 86,
  - 5th line from top, before the first "if", add: "(i.e., for every neighborhood V of y in  $S_2$ , there exists a neighborhood U of x in  $S_1$  such that  $f(t) \in V$  whenever  $t \in U$ )"

• 7th line from top, before "and", add: "(i.e., 
$$\lim_{t \to a} f(t) = f(a)$$
)"

- 32. p. 87, in Exercise 213
  - Item (v), 3rd line: suppress "general"
  - Item (viii, b), 3rd line: supress "a"
- 33. p. 88, 3rd line from bottom: add a hyphen between "group" and "homomorphism
- 34. p. 92, 5th line from bottom: suppress once "GCD, EDR"
- 35. p. 93,
  - in Remark 220(b), 1st line, change "properties (ii)" to "property (i) of Definition 218"
  - in Definition 221, at the end of the second line, add "where  $n1 \triangleq 1 + \ldots + 1$  (*n* times)"
- 36. p. 107, 9th line from top: change "jth" to "ith"

37. p. 110, 6th line from bottom, change the expression  $\beta_i = \sum_{1 \le i \le n} p_{ij} \alpha_i$ 

to 
$$\beta_i = \sum_{1 \le j \le n} p_{ij} \alpha_j$$

- 38. p. 129, 6th line from bottom: delete 340
- 39. p. 137, 4th line from bottom: after " $\partial_k$ ", add "is"
- 40. p. 138,
  - 9th line from top: change "makes sense" to "holds"
  - 11th line from top: change s to  $\mathfrak{s}$  and s' to  $\mathfrak{s}'$
- 41. p. 139, 1st line of the proof of Theorem 362, before "(i):", add "We proceed by contradiction."
- 42. p. 141,
  - 2nd line from top, delete "(i)"
  - 4th line from top, change "quotient division ring" to "division ring of fractions"
- 43. p. 142, 13th line from top, after the parenthesis, add "for i = 0"
- 44. p. 144, 4th line from bottom, change P to  $P_N$
- 45. p. 146, 2nd line from top: multiply the right-hand member of the equality by  $(-1)^N$
- 46. p. 149, end of the proof of Theorem 383: close the parenthesis
- 47. p. 152, 9th line from top: change "Jacobson ideal" to "Jacobson radical".
- 48. p. 153, 3rd line from top: read "V.1" instead of "VI.1"
- 49. p. 181,
  - 2nd line from bottom: change "and V" to ". (i) Let V be"
  - 1st line from bottom: add the following to the last sentence: (ii) Let  $u : \mathbf{K} \to \mathbf{K}$  be a homomorphism. Prove that u is injective. (Hint: use Theorem 227 and Lemma 232.)
- 50. p. 185, 7th line from top: change  $X \lambda$  to  $t \lambda$
- 51. p. 204,
  - 6th line, change xa by = 1 to ax yb = 1
  - 5th line of Corollary 529: change (a, b) to (b, a) and "right-" to "left-"
  - 3rd line from bottom: change (a, b) to (b, a)
  - 2nd line from bottom: change ab = b'a' to ba = a'b', and (a', b) to (b, a'), and "right-" to "left-"

- 1st line from bottom: change "(a', b) is strongly right-" to "(b, a') is strongly left-"
- 52. p. 205, 1st line from top: change ab = b'a' to ba = a'b'
- 53. p. 272, lines 6 and 7 of the proof of Theorem 707:
  - delete "we have ... Therefore,"
  - after "is injective", add "(Exercise 472(ii))"
- 54. p. 274, lines 6, 13 and 21 from top: change "monomorphism" to "homomorphism"
- 55. p. 287, 3rd and 8th line of Theorem 752, change

• 
$$X^n + p_1 X^{n-1} + \dots + p_n$$
 to  $X^n - p_1 X^{n-1} + \dots + (-1)^n p_n$   
•  $X^n + p_1 A^{n-1} + \dots + p_n I_n$  to  $X^n - p_1 A^{n-1} + \dots + (-1)^n p_n I_n$ 

56. p. 298,

- 1st line of the proof of Lemma 777: change "(i) and" to "(i) is proved in ([28], §V.16, Theorem 1)."
- $\bullet\,$  delete the last sentence of the 1st § of the proof
- at the beginning of the 2nd §, suppress "(1)"
- delete lines 12 to 15
- delete  $\S(2)$  of the proof
- 57. p. 315, 4th line of Prop. 810, in the brackets: change  $\mathcal{S}$  to  $\mathcal{S}_k$
- 58. p. 346, 9th line of Theorem and Definition 863, after afer "observable image representation", add ", i.e. there exists an **E**-linear bijection  $\overline{(S \bullet)}$  :  ${}^{r}W \xrightarrow{\sim} \mathfrak{B}_{W}(M)$  induced by the **E**-linear injection  $(S \bullet)$  :  ${}^{r}W \xrightarrow{\sim} {}^{k}W$  "
- 59. p. 360,
  - Instead of the 4 last lines of Proposition 881, read the following: "The following conditions are equivalent:
    - (i) M is strongly controllable;
    - (ii) M is controllable;
    - (iii) M is Kalman-controllable;
    - (iv) there exists an integer  $s \geq 1$  such that  $\operatorname{rk}_{\mathbf{k}} \Gamma_{s}(t_{0}) = n;$
    - (v) there exists a discrete subset S of  $\Omega$  such that  $\operatorname{rk}_{\mathbf{k}}\Gamma_{n}(t) = n$  for all  $t \in \Omega \setminus S$ ."

- In the proof of Proposition 881,
  - (a) 3rd line from top, instead of "(i)(a)", read "(ii)⇒(iii) by Theorem and Definition 879(3).
    (iii)⇒(iv):"
  - (b) 5th line from bottom, instead of "(b)", read "(iv) $\Rightarrow$ (iii):"
  - (c) Last line, instead of "For (ii)", read "(iii) $\Leftrightarrow$ (v):"
  - (d) At the end of the proof, the following is added: "(v) $\Rightarrow$ (i): (iv) holds if, and only if there exists a submatrix  $\Delta_n(t)$  of  $\Gamma_n(t)$ , consisting of n columns of  $\Gamma_n(t)$ , such that  $|\Delta_n(t)| \neq 0$  for all  $t \in \Omega \setminus S$ . This means that the analytic function  $t \mapsto |\Delta_n(t)|$  is nonzero, i.e.  $\operatorname{rk}_{\mathbf{K}} \Delta_n = \operatorname{rk}_{\mathbf{K}} \Gamma_n \neq 0$ . Therefore, (i) holds by Theorem and Definition 879(2)."
- 60. p. 390, in Exercise 939, after the end of the 2nd sentence, add: "(Hint: use Theorem and Definition 185(ii).)"
- 61. p. 396, in Part (ii) of Exercise 956, read " $\Omega$ " instead of " $\Omega \setminus S$ "
- 62. p. 390, in Exercise 935, add after the last line: "(Hint: show that  $\bar{P} \to P \delta_x$ , where  $\bar{P} = P + \mathfrak{m}$ , is an isomorphism.)"
- 63. p. 400,
  - 10th line from bottom: at the end of the sentence, the following is added: "and Ilchmann *et al.* [163]"
  - 9th line from bottom: this sentence is deleted
- 64. p. 415, Definition 982, replace  $\chi(f) = a$  by  $\chi[f] = a$
- 65. p. 416, Theorem 425: in the last line, read "not exponentially stable" instead of "exponentially unstable"
- 66. 420, Definition 990: To be coherent with the definition in the literature (see, e.g., [286]),  $\partial$  should be replaced by  $\delta = t\partial$
- 67. p. 452: line 8 from bottom: read  $\{-a\}$  instead of  $\{a\}$
- 68. p. 425, lines 14 and 16 from top: replace  $\check{\mathbf{K}}$  and  $\breve{\mathbf{K}}$  by  $\widetilde{\mathbf{K}}$
- 69. p. 426, line 1 from top: replace  $a_n$  by  $a_m$
- 70. p. 443, Section 6.7.1:
  - after the first sentence add: Laurent polynomials in the indeterminate q must be used for Theorem 367 to apply (simplicity of the ring  $\mathbf{T}$ )
  - $\bullet\,$  delete the last sentence of the first paragraph

71. p. 630, 25th line from top: delete the entry "stably free"